

$$\begin{aligned}
 W^{\text{out}}(C,A) &= OA/(OA+OB+OD) &= 3/6 \\
 &= 2/(2+3+1) &= 1/2 \\
 &= 2/6 & \\
 &= 1/3 & \\
 W^{\text{in}} & & \\
 (D,A) &= IA/(IB+IC) & \\
 &= 3/(2+2) & \\
 &= 3/4 & \\
 W^{\text{out}} & & \\
 (D,A) &= OA/OA & \\
 &= 2/2 & \\
 &= 1 & \\
 \end{aligned} \tag{8}$$

$$\begin{aligned}
 W^{\text{in}}(B,C) &= IC/(IA+IB) & \\
 &= 2/(3+2) & \\
 &= 2/5 & \\
 W^{\text{out}}(B,C) &= OC/(OA+OC+OD) & \\
 &= 3/(2+3+1) & \\
 &= 3/6 & \\
 &= 1/2 & \\
 \end{aligned} \tag{9}$$

$$\begin{aligned}
 W^{\text{in}}(B,D) &= ID/(IB+IC) & \\
 &= 2/(2+2) & \\
 &= 2/4 = 1/2 & \\
 W^{\text{out}}(B,D) &= OD/OA & \\
 &= 2/2 & \\
 &= 1 & \\
 \end{aligned} \tag{10}$$

Now these in links and out links weight, equation numbers (5, 6, 7, 8, 9, 10) are put in the Equation (4) to calculate the weighted rank of the nodes A, B, C, and D as following:

$$WPR(B) = (1-d) + d \sum WPR(A) W^{\text{in}}(A,B) W^{\text{out}}(A,B) + WPR(C) W^{\text{in}}(C,B) W^{\text{out}}(C,B) \tag{11}$$

$$WPR(C) = (1-d) + d \sum WPR(A) W^{\text{in}}(A,C) W^{\text{out}}(A,C) + WPR(B) W^{\text{in}}(B,C) W^{\text{out}}(B,C) \tag{12}$$

$$WPR(D) = (1-d) + d \sum WPR(B) W^{\text{in}}(B,D) W^{\text{out}}(B,D) + WPR(C) W^{\text{in}}(C,D) W^{\text{out}}(C,D) \tag{13}$$

For WPR(A) calculation the value of d is set to 0.85(standard value) and the initial values of WPR(B), WPR(C) and WPR(D) is considered 1, so calculation for 1st iteration as follows:

$$WPR(A) = (1 - 0.85) + 0.85(1 * 3 / 5 * 1/3 + 1 * 3 / 5 * 1/3 + 1 * 3 / 4 * 1) = 1.127 \tag{14}$$

$$\begin{aligned}
 W^{\text{in}}(A,B) &= IB/(IB+IC+ID) \\
 &= 2/(2+2+2) \\
 &= 2/6 \\
 &= 1/3 \\
 \end{aligned} \tag{15}$$

$$\begin{aligned}
 W^{\text{out}}(A,B) &= OB/(OB+OC) \\
 &= 3/(3+3) \\
 &= 3/6 \\
 &= 1/2 \\
 \end{aligned} \tag{16}$$

$$\begin{aligned}
 W^{\text{in}}(C,B) &= IB/(IA+IB) \\
 &= 2/(3+2) \\
 &= 2/5 \\
 \end{aligned} \tag{17}$$

$$\begin{aligned}
 W^{\text{out}}(C,B) &= OB/(OA+OB+OD) \\
 &= 3/(2+3+1) \\
 &= 3/6 \\
 &= 1/2 \\
 \end{aligned} \tag{18}$$

Again now for calculation of WPR (B) these equations (15, 16, 17, and 18) are put in to equation (11).

In this the initial value of WPR(C) is set to 1.

$$\begin{aligned}
 WPR(B) &= (1 - 0.85) + 0.85(1.127 * 1/3 * 1/2 + 1 * 2/5 * 1/2) \\
 &= (0.15) + 0.85(1.127 * 0.33 * 0.50 + 1 * 0.40 * 0.50) \\
 &= 0.4989 \\
 \end{aligned} \tag{19}$$

$$\begin{aligned}
 W^{\text{in}}(A,C) &= IC/(IB+IC+ID) \\
 &= 2/(2+2+2) \\
 &= 2/6 \\
 &= 1/3 \\
 \end{aligned} \tag{20}$$

$$\begin{aligned}
 W^{\text{out}}(A,C) &= OC/(OB+OC) \\
 &= 3/(3+3) \\
 \end{aligned}$$

By substituting the values of equations (14), (19), (20), (21), (22) and (23) to equation (12), you will get the WPR of Page C by taking d as 0.85.

$$\begin{aligned}
 WPR(C) &= (1 - 0.85) + 0.85((1.127 * 1/3 * 1/2) + (0.499 * 2 / 5 * 1/2)) \\
 &= (0.15) + 0.85((1.127 * 0.33 * 0.50) + (0.499 * 0.40 * 0.50)) \\
 &= 0.392 \\
 \end{aligned} \tag{24}$$

$$\begin{aligned}
 W^{\text{in}}(B,D) &= ID/(IB+IC) \\
 &= 2/(2+2) \\
 &= 2/4 = 1/2 \\
 \end{aligned} \tag{25}$$

$$\begin{aligned}
 W^{\text{out}}(B,D) &= OD/OA \\
 &= 2/2 \\
 &= 1 \\
 \end{aligned} \tag{26}$$

$$\begin{aligned}
 W^{\text{in}}(C,D) &= ID/(IA+IB) \\
 &= 2/(2+3) \\
 &= 2/5 \\
 \end{aligned} \tag{27}$$

$$\begin{aligned}
 W^{\text{out}}(C,D) &= OD/(OA+OB+OD) \\
 &= 2/(2+3+1) \\
 &= 2/6 \\
 &= 1/3 \\
 \end{aligned} \tag{28}$$

Again by substituting the values of equations (19), (24), (25), (26), (27) and (28) to equation (13), you will get the WPR(D) by taking d as 0.85.

$$\begin{aligned}
 WPR(D) &= (1 - 0.85) + 0.85((0.499 * 1/2 * 1) + (0.392 * 2 / 5 * 1/3)) \\
 &= (0.15) + 0.85((0.499 * 0.50 * 1) + (0.392 * 0.40 * 0.33)) \\
 &= 0.406 \\
 \end{aligned} \tag{29}$$

The values of WPR(A), WPR(B), WPR(C), WPR(D) are demonstrated in equations (14), (19), (24) and (29) consequence. The association between these are WPR(A) > WPR(B) > WPR(D) > WPR(C).

Iteration	A	B	C	D
1	1	1	1	1
2	1.1275	0.47972	0.3912	0.19935
3	0.425162	0.27674	0.25727	0.18026
4	0.355701	0.244128	0.24189	0.177541
5	0.34580	0.247110	0.239808	0.17719
6	0.34454	0.23957	0.23953	0.17714
7	0.34438	0.23950	0.23950	0.17714
8	0.34436	0.23950	0.23949	0.17714

Iterative calculations values for weighted page rank

6. Experiments

To evaluate the WPR algorithm, we implemented WPR and the standard Page Rank algorithms to compare their results. The different Components involved in the execution and assessment of the WPR algorithm are illustrated in Figure 1. It consists of six major activities to be carried out in order to perform simulation studies in this work.

1. Finding a web site: The standard Page Rank and the WPR Algorithm are relying on the web structures so it is significant to find out a website with rich hyperlinks. The Website of Saint Thomas University, in Fredericton, has been chosen after comparing the structures of the various websites.

2. Building a web map: A free spider software—J Spider—is used to generate the web map because the website does not consist of the required Web map.

3. Finding the root set: Using the IR search Engine, which is encapsulated in the website a set of the pages called root set has to be retrieved relevant to the given Query.

4. Finding the base set: By expanding the root set with pages which directly points to or pointed to the pages in the root set, then a base set is created

5. Applying algorithms: Applying of Standard Page Rank and WPR algorithm to the base set.

6. Evaluating the results: Execute the algorithm by comparing their results.

7. Evaluation

To Evaluating the Standard Page Ranking and Weighted Page Ranking algorithm using the “Travel Agent” and “Scholarship” query topics. Travel agent” represents a non-focal point whereas “scholarship” represents a focal (popular) point in the Website of Saint Thomas University. The results of the evaluation are summarizing in the following subsections.

6.1. The determination of the relevancy of the pages to the given query

The Standard Page Rank and the WPR algorithms provide important information about a given query by using the structure of the website. We categorized the pages in the results into four classes based on their applicability to the given query:

- **Very Relevant pages (VR)**, which contain very important information about the given query,
- **Relevant pages (R)**, which have relevant but not important information about the given query,
- **Weak-Relevant pages (WR)**, which do not have relevant information about the given query even though they contain the keywords of the given query, and
- **Irrelevant pages (IR)**: which include neither the keywords of the given query nor relevant information about it.

6.2. The Calculation of the relevancy of the page lists to the given query

The performances of the WPR and the standard Page Rank algorithms have been evaluated to identify the algorithm that produces better results.

Table 1: the relevancy values for the query “travel agent” produced by PageRank and WPR using different page sets

Size of page set	Number of Relevant Pages		Relevancy Value(k)	
	PageRank	WPR	PageRank	WPR
10	0	1	0.1	0.5
20	4	3	13.1	16.8
30	4	4	47.1	49.8
40	4	4	82.1	84.8
50	4	4	117.1	119.8
60	5	5	159.6	162.3
70	7	7	211.7	214.4

6.3. Focused Topic Queries

This subsection evaluates the results obtained for the query “scholarship.” The relevancy values of the results are shown in Table 2. Similar to the query “travel agent,” (larger relevancy values) for the query “scholarship.” Moreover, the two points derived from the query “travel agent” are shown more clearly in this case (see Table 2).

In conclusion, the results obtained from WPR and standard PageRank for the focused and non-focused topics show that WPR is superior to standard PageRank. In this utilize, we make a hierarchic tip of people's cant and leave the being identification difficulty to users. With a returned figure itemise, users can identify experts by searching their defamation together with the ask substance finished a web examine engine. We also use a set of calumny extracted from DBLP to conductor the reput extraction difficulty, which is certainly a main investigate job.

Table 2: The relevancy values for the query “scholarship” produced by PageRank and WPR using Different page sets

Size of the page set	Number of Relevant Pages		Relevancy Value(κ)	
	PageRank	WPR	PageRank	WPR
5	2	3	2	5.5
10	2	4	9.5	22
20	4	4	34.5	57
30	8	5	87.5	99
40	10	8	158.5	159.3
80	16	15	624.8	655.3
100	22	19	999.2	1045.3
120	25	20	1470.4	1473.3

6.3 Rank Updater

In this module, rank score of the returned page is improved by applying the input of the query processor and matched documents of a user query. It operated online and applied the improvements to the concerned documents.

Step 1: Given an input query q and matched documents D collected from the query processor, the webpage is found to which the query q belongs.

Step 2: The level weight are calculated for every page X present in the sequential pattern.

Step 3: The rank are calculated for every page X present in the sequential pattern. The improved is calculated as the summation of pervious rank and assigned weight value.

Due to the optimization of the Search engine results, the rank will improve so that it will serve the user need by providing the popular and relevant pages upwards in the result list.

8. Experimental Result

Table 3: Experimental result

Size of the paper set	Number of Relevant Pages		Relevancy Value(X)		New Relevancy Value (PageRank + WPR)
	PageRank	WPR	PageRank	WPR	
10	0	1	0.1	0.5	0.6
20	4	3	13.1	16.8	29.9
30	4	4	47.1	49.8	96.9
40	4	4	82.1	84.8	166.9
50	4	4	117.1	119.8	236.9
60	5	5	159.6	162.3	321.9

9. Conclusion

Web mining is used to retrieve information from users' past behavior. In this approach, Web structure mining plays a major role. Two commonly used algorithms in web structure mining are HITS and Page Rank, which are used to rank the relevant pages. When distributing the rank scores both algorithms will be treat the links equally. To improve the performances of this method so many algorithms are introduce. This paper introduces the WPR algorithm, an extension to the Page Rank algorithm. Based on the importance of the in links and out links of the pages the rank scores are distributing using the popularity of the pages in the WPR algorithm. Saint Thomas University shows that WPR is able to identify a larger number of relevant pages to a given query compared to standard Page Rank. This algorithm is improving the order of the page in the result list so that the user gets the relevant and important pages in the list.

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