

# Effect of Different Inter-Electrode Distances on Order-to-Chaos-to Order Transitions in Co-Axial Electrode DC Glow Discharge

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**Abstract:** This paper attempts to understand the role of the electrode dimensions in the evolution of order-to-chaos-to-order transitions in a co-axial DC electrode discharge system, wherein the ratio of the anode-to-cathode radii is observed to determine the evolution path of the transition. Further the anode dimensions is observed to determine the discharge conductivity after the 1<sup>st</sup> negative differential resistance (NDR) region and the onset of the order-to-chaos-to-order transition is linked to the cathode dimensions.

**Keywords:** DC discharge characteristics, negative differential resistance, floating potential oscillations and dynamical changes in the system

## 1. Introduction

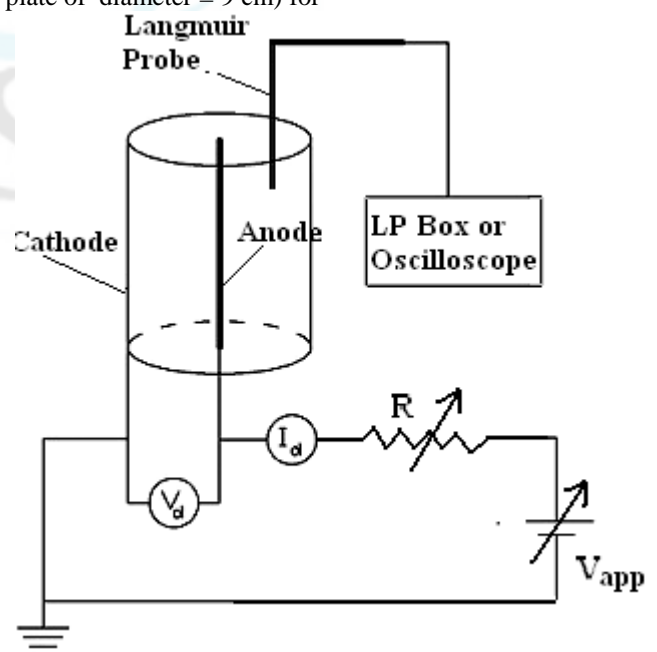
Plasma discharges being a nonlinear medium, observations of associated hysteresis effects at negative differential regions (NDR) are signatures of the nonlinear dynamical evolution of the system. Such hysteresis loops are quite commonly observed near the Townsend breakdown and abnormal glow discharge regions of a planar electrode DC plasma discharge. However, there have also been observations of NDR regions in discharge [discharge current versus bias voltage] characteristics of systems such as the DP machine [1] and coaxial electrode geometry [discharge current ( $I_d$ ) versus discharge voltage ( $V_d$ ) characteristics] systems [2], in which the dynamical evolution of the system has been characterized using fluctuation signals [2-6] obtained from the plasma. In different systems and under different operating conditions, the fluctuation signals have been observed to undergo order-to-chaos [7] as well as chaos-to-order [8, 9] transitions. Order-to-chaos-to-order transitions [2, 10] have also been observed recently.

As reported earlier, the  $I_d$ - $V_d$  characteristics [2, 11, 12] of the DC coaxial electrode discharges with a powered central anode have been observed to have two consecutive negative differential resistance (NDR) regions. The 1<sup>st</sup> NDR has been observed to be correlated to an upper voltage threshold whereas the 2<sup>nd</sup> NDR is seen to be linked to the discharge current [11]. The voltage drop across the 1<sup>st</sup> NDR is seen to trigger relatively large amplitude floating potential oscillations in comparison to those prior to the 1<sup>st</sup> NDR region. These oscillations, thereafter, are seen to undergo an order-to-chaos-to-order transition with increasing discharge current. As the  $I_d$  -  $V_d$  characteristic behavior seems to be linked to the polarity direction of the electrode configuration, the role of the dependence on the electrode geometry seems to be an important factor.

This paper reports the discharge characteristics and evolution of the system in co-axial electrode geometry with different inter-electrode distances, by varying the diameters of the anode/cathode.

## 2. Experimental Setup

The experimental setup (Fig. 1) consists of a coaxial stainless steel electrode system ( $\approx 6$  cm long), with the central axial rod (diameter  $\approx 0.15$  cm) being the powered anode and the outer cylindrical tube (inner diameter  $\approx 4.8$  cm) acting as the grounded cathode. The coaxial electrode system rests on a teflon platform at a height of 16 cm from the base of the vacuum chamber (I.D. = 15.0 cm, height = 38.3 cm), in which the electrode system is enclosed. The teflon is shielded from direct contact with the plasma by using a thin mica sheet. The top end of the electrode system is open. The pumping section is at the bottom of the vacuum chamber whereas the top flange has a viewing port (quartz plate of diameter = 9 cm) for



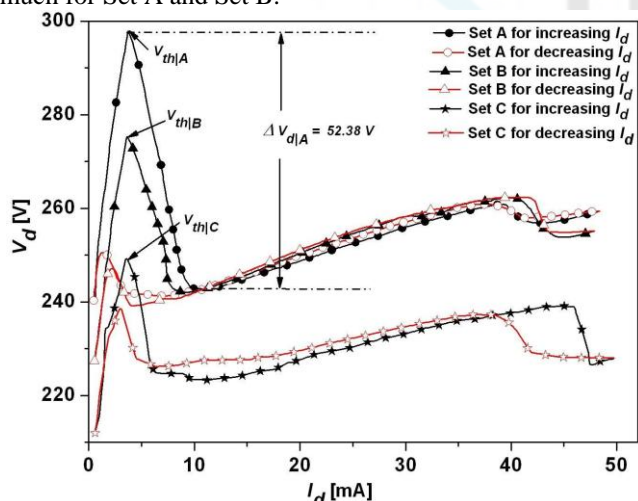
**Figure 1:** A schematic diagram of the electrode system and external circuit connection. The location of insertion of the Langmuir probe is also shown

carrying out spectroscopic measurements and taking plasma images. The vacuum chamber has three side ports (each of diameter  $r = 6$  cm) at a height of 27 cm from the base of the chamber. One of the side ports is used for inserting the Langmuir probe (as shown in Fig 1) and another is used as an Argon (Ar) gas inlet port with the vacuum gauges (Micro-Pirani and capacitance manometer) mounted on the third side port. The external circuit is completed through a variable DC power supply (1 kV, 1 A), variable resistances and an ammeter.

### 3. Experimental Results and Discussion

In this paper, experiments have been carried out with central anode diameters of 1.5 mm and 12 mm and outer diameters of the grounded cathode being 50 mm and 70 mm, thickness of 1 mm. Experimental results from three different inter-electrode distances [viz., (1.5, 50), (1.5, 70) and (12, 70)] with an anode to cathode radii ratio of (1/33), (1/47) and (1/6) respectively are presented in this paper. The three configurations are henceforth called Set A, Set B and Set C respectively. A single Langmuir probe has been used for plasma parameter radial profile measurements at an operating pressure of 850 mTorr.

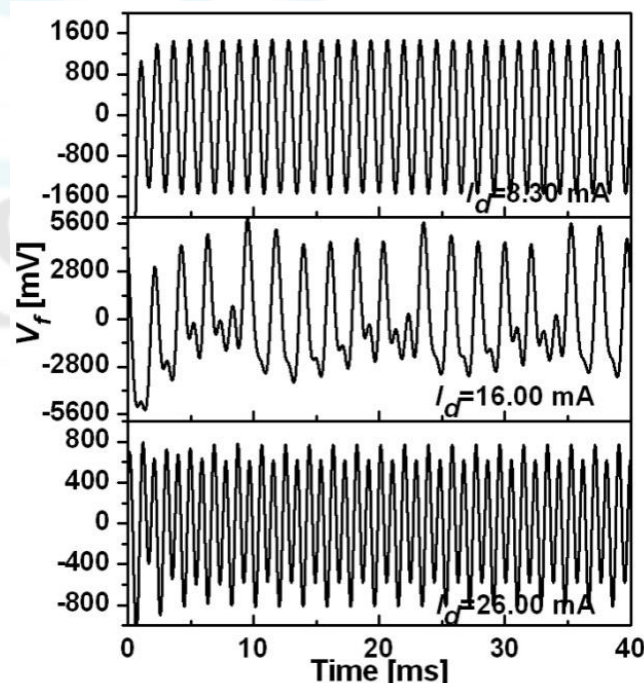
Fig. 2 shows the  $I_d$ - $V_d$  characteristics, both for increasing and decreasing currents, for the three different inter electrode distances. The voltage threshold voltage ( $V_{th}$ ) at which the 1<sup>st</sup> NDR occurs is seen to decrease with an increase in the cathode/anode diameters, with the threshold dropping from 297 V to 273 V to 250 V in Set A, B and C electrode configurations respectively. It is interesting to note that the discharge current at which the 1<sup>st</sup> NDR is triggered is the same (~3.5 mA). The dominant effect is observed when the anode rod diameter is increased. The voltage drop ( $\Delta V_d$ ) across the 1<sup>st</sup> NDR is seen to decrease from 53 V to 35 V to 25 V. It is further observed that the conductivity of the system after the first NDR seems to increase with change in the central anode diameter, as seen by the sustenance of the discharge at a lower discharge voltage for Set C configuration, which however, does not seem to change much for Set A and Set B.



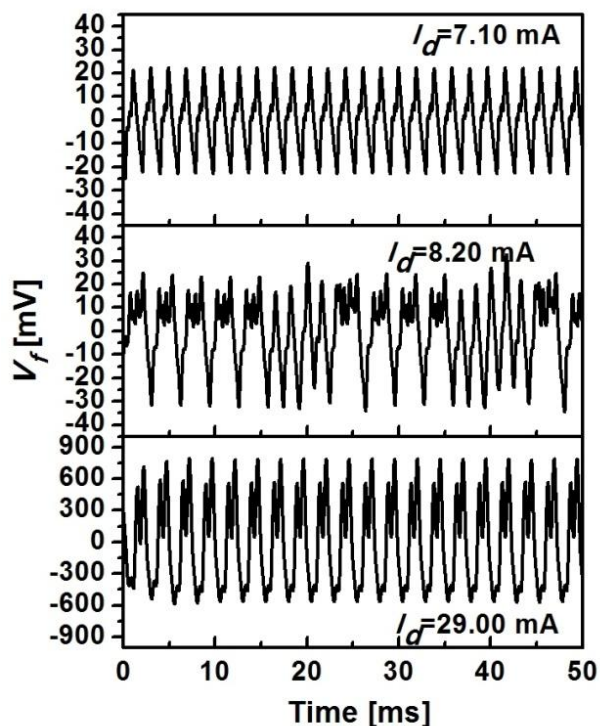
**Figure 2:**  $I_d$ - $V_d$  discharge characteristics for increasing (black) and decreasing (red)  $I_d$  for different inter-electrode distances at  $p=850$  mTorr.  $V_{th/A}$ ,  $V_{th/B}$  and  $V_{th/C}$  are the threshold voltages at 1<sup>st</sup> NDR for Set A, B & C respectively.  $\Delta V_{d/A}$  is the voltage drop across the 1<sup>st</sup> NDR for Set A.

The region between the 1<sup>st</sup> NDR and 2<sup>nd</sup> NDR is seen to undergo an order-to-chaos-to-order transition [2, 10] in the floating potential oscillations. Similar features have been observed for all the different electrode configurations reported here. However, the regions of onset of this transition and their behaviour are not same for all the configurations. Figs. 3, 4 and 5; show three representative oscillations, for each of the Sets A, B & C, depicting an order-to-chaos-to-order transition as one increases  $I_d$ . It is to be noted that oscillations at other  $I_d$ 's have also been recorded but not shown here.

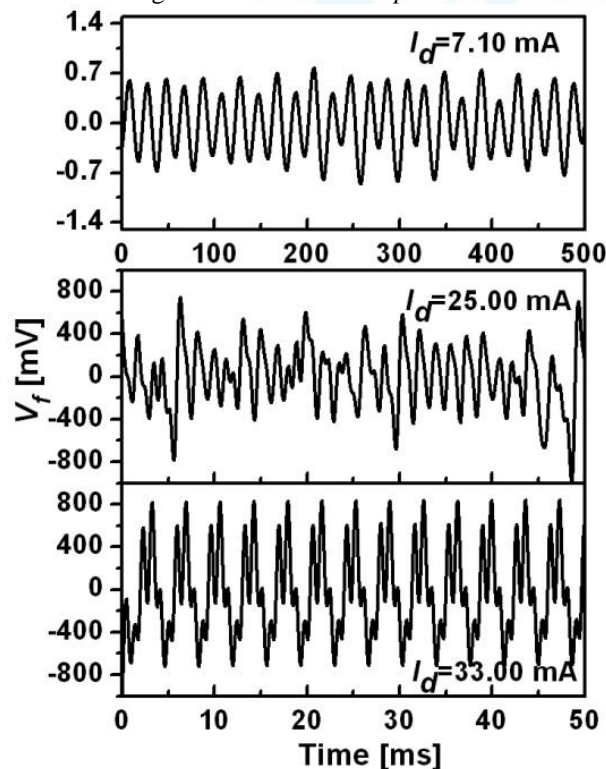
For Set A, it is observed that after the 1<sup>st</sup> NDR, the oscillations have an ordered behaviour from  $I_d \approx 8.34$  mA to 15.9 mA whereas the chaotic zone is from  $I_d \approx 16.0$  mA to 18.0 mA. Thereafter the oscillations remain ordered up to the maximum discharge current (46.0 mA) recorded. For Set B, the oscillations show order at  $I_d \approx 7.10$  mA, just after the 1<sup>st</sup> NDR. These remain ordered up to 8.10 mA of  $I_d$  value. The chaotic zone is observed to widen from  $I_d \approx 8.20$  mA to 28.8 mA. The oscillations at  $I_d \approx 29.0$  mA is observed to be ordered. At  $I_d \approx 31.10$  mA and  $I_d \approx 33.0$  mA, the system again becomes chaotic. At  $I_d \approx 35.5$  mA, it is ordered again. At  $I_d \approx 37.0$  mA to 42.0 mA, the system is chaotic. As the control parameter limit is reached, the system becomes ordered again (i.e. between  $I_d \approx 42.8$  mA to 45.0 mA). Thus it is seen that in this configuration, the system traverses the order-chaos-order path again and again. In Set C, the oscillations depict order in the current range  $I_d \approx 7.10$  mA to 24.5 mA whereas from  $I_d \approx 25.0$  mA to 29.0 mA, it is chaotic and thereafter at higher  $I_d$ 's, the system tends to become ordered as  $I_d$  is increased to 48.0 mA.



**Figure 3:** Floating potential oscillations for increasing discharge current for Set A at  $p=850$  mTorr.



**Figure 4:** Floating potential oscillations for increasing discharge current for Set B at  $p=850$  mTorr.



**Figure 5:** Floating potential oscillations for increasing discharge current for Set C at  $p=850$  mTorr.

#### 4. Characterizations of Fluctuations

The onset of the chaos-order-chaos region and its evolution pattern seems different and thus a basic characterization of these fluctuations were carried out with respect to  $I_d$ . The amplitude bifurcation of the oscillations shown in Fig. 6 for Sets A, B and C show that the onset of the chaotic region starts at higher and higher  $I_d$  values as one shows from Set A to Set B to Set C configurations respectively. The current jump is more significant from Set A to Set B. Further, the behavior of the bifurcation diagram seems to evolve differently in the three cases, with the system tending to become ordered more slowly when the inter electrode distance is maximum (Set B).

The amplitude levels also show an interesting trend. As seen in Set B of Fig. 6, at  $I_d \approx 21.3$  mA, the amplitude of oscillations suddenly increase and tends to remain in this increased level up to  $I_d \approx 31.10$  mA. Thereafter at  $I_d \approx 33.0$  mA, the amplitude levels of oscillations show a decreasing trend till the control parameter limit. Comparing this with Set A and Set C, one finds in these sets that the large amplitude phenomenon tends to decrease relatively faster after a certain current limit with the amplitudes remaining at lower levels ( $\sim 20$  mV). Thereafter, the amplitude decay rate is slightly slower in Set C as compared to Set A. It may be possible that one observes such reduction in amplitude levels at higher  $I_d$  in Set B also but at present the experimental set up does not have the facility to go to such high discharge currents.

In order to understand the deviation of the oscillations from the DC level, their variance has been estimated (Fig. 7) which reveals that the variance is large in the region of the chaotic regions and hence onset of maximum variance tends to shift to the right i.e. linked to the onset of the order-to-chaos-to-order transition with the largest shift being observed when the cathode diameter is changed (i.e. Set A to Set B/C) as observed in Fig. 5 also.



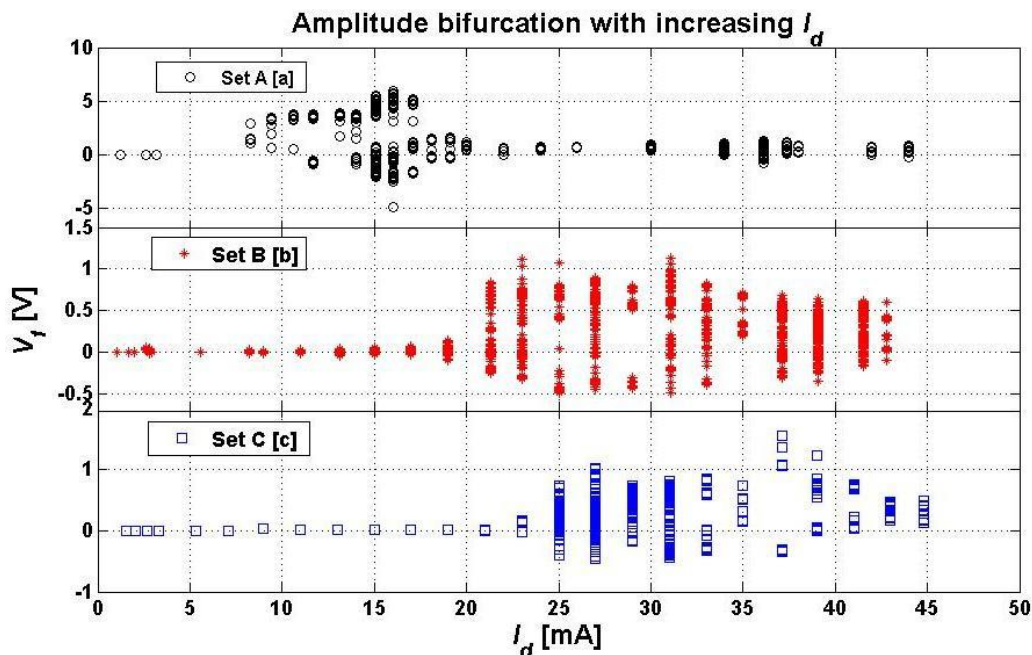


Figure 6: Amplitude bifurcation diagram from the different electrode dimensions at  $p= 850$  mTorr: (a) Set A, (b) Set B, and (c) Set C.

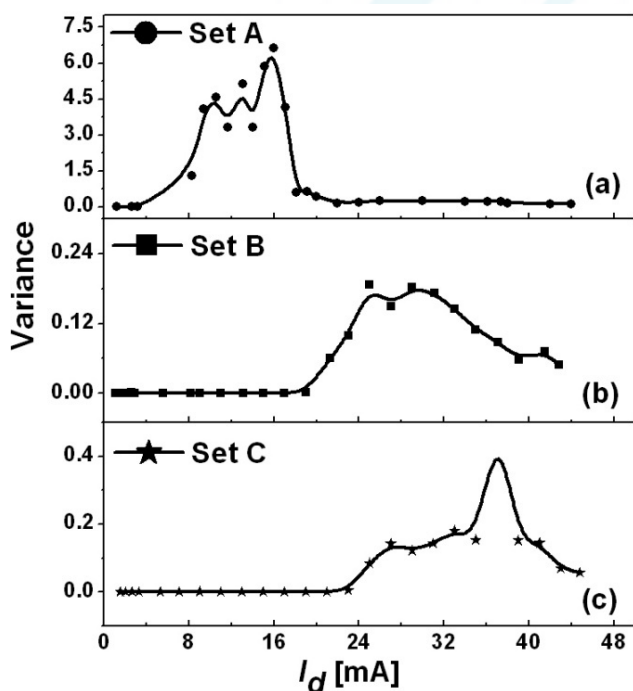


Figure 7: Variance versus  $I_d$  for the different electrode dimensions at  $p= 850$  mTorr: (a) Set A, (b) Set B, and (c) Set C.

### 5. Conclusion

The changes in the onset of the 1<sup>st</sup> NDR when one characterizes Set A, Set B and Set C configuration; show that the NDR is triggered at significantly higher conductivity as the electrode surface area is increased and the system transits to a significantly higher conducting state after 1<sup>st</sup> NDR when the anode diameter is changed. However, the onset of the order-to-chaos-to-order transition seems to be governed by the cathode dimensions. Further it needs to be stated that the evolution of the order-to-chaos-to-order zone

seems depend on a critical value of the ratio of anode-to-cathode radii which needs to be investigated further.

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