Volume 2 Issue 3, March 2014

Trajectory Tracking of a 2-Link Robotic Manipulator Using Adaptive Terminal Sliding Mode Controller

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Abstract: This paper proposes an adaptive terminal sliding mode controller which combines adaptive control and sliding mode control to control a 2-link nonlinear robotic manipulator with uncertain parameters. We use an adaptive algorithm based on the concept of sliding mode control to alleviate the chattering phenomenon of control input. Adaptive laws are developed to obtain the gain of switching input and the boundary layer parameters. The stability and convergence of the robotic manipulator control system are guaranteed by applying the Lyapunov stability theorem. Simulation results demonstrate that the chattering of control input can be alleviated effectively. The proposed controller scheme can assure robustness against a large class of uncertainties and achieve good trajectory tracking performance.

Keywords: Robotic manipulators, sliding mode control, adaptive law, Lyapunov stability theorem

1.Introduction

A chattering free adaptive terminal sliding mode controller for uncertain systems is proposed in this paper. The actual control law is obtained by integrating the discontinuous derivative control signal and hence it is continuous. The sliding mode control is based on the design of a high-speed switching control law that drives the system's trajectory onto a user-chosen hyperplane in the state space, also known as sliding surface. The main feature of sliding mode control are the following: (1) fast response and good transient performance; (2) robustness against a large class of perturbations or model uncertainties; and (3) the possibility of stabilizing some complex nonlinear systems which are difficult to stabilize by state feedback control laws. Chattering phenomenon can cause some problems such as saturation and heat for mechanical parts of robot manipulators or drivers. To reduce or eliminate the chattering, various papers have been reported by many researchers and classified in two most important methods, namely, boundary layer saturation method and estimated uncertainties method. Non linear control methodologies are more general because they can be used in linear and non linear systems. These controllers can solve different problems such as, invariance to system uncertainties and resistance to the external disturbance. The most common non linear methodologies that have been proposed to solve the control problem consist of the following methodologies:

- Feedback Linearization Control Methodology
- Passivity-Based Control Methodology
- Sliding Mode Control Methodology
- Robust Lyapunov-Based Control Methodology
- Adaptive Control Methodology
- Artificial Intelligence-Based Methodology

The requirement of prior knowledge about the uncertainty bands for designing terminal sliding mode controllers is not a

necessary requirement in the proposed controller. Trajectory tracking of a 2-link robotic manipulator which is a non-linear system with mismatched uncertainties also considered in our simulation study. Simulation results demonstrate that the proposed control strategy is successful in eliminating the undesired chattering in the control input while ensuring satisfactory stabilization as well as tracking performances. Hence the proposed controller is suitable for practical applications.

2. Description

2.1 Tracking Control of a Robotic Manipulator

Dynamics of an n-link robotic manipulator can be expressed as, $M(q)\ddot{q} + C(q, \dot{q})\dot{q} + G(q) = \tau + \tau_{d} (1.0)$

where q, \dot{q} , $\ddot{q} \in \mathbb{R}^n$ represent the position, velocity and acceleration of the joints respectively,

$$\begin{split} \mathbf{M}(\mathbf{q}) &= \mathbf{M}_{\mathbf{0}}(\mathbf{q}) + \Delta \mathbf{M}(\mathbf{q}) \in \mathbf{R}^{n \times n} \text{ stands for the inertia matrix,} \\ \mathbf{C}(\mathbf{q}, \dot{\mathbf{q}}) &= \mathbf{C}_{\mathbf{0}}(\mathbf{q}, \dot{\mathbf{q}}) + \Delta \mathbf{C}(\mathbf{q}, \dot{\mathbf{q}}) \in \mathbf{R}^{n \times n} \end{split}$$

is the centripetal Coriolis matrix, $G(q) = G_0(q) + \Delta G(q) \in \mathbb{R}^n$ is the gravitational vector, $\tau \in \mathbb{R}^n$ is the joint torque vector and $\tau_d \in \mathbb{R}^n$ is the disturbance torque vector. Here $M_0(q)$, $C_0(q, \dot{q}), G_0(q)$ are the nominal terms and $\Delta M(q), \Delta C(q, \dot{q}), \Delta G(q)$ represent the perturbations in the system matrices.

Then the dynamic model of the robotic manipulator can be written as,

 $\begin{aligned} \boldsymbol{M}_{0}(\mathbf{q})\boldsymbol{\ddot{q}} + \boldsymbol{C}_{0}(\mathbf{q}, \boldsymbol{\dot{q}})\boldsymbol{\dot{q}} + \boldsymbol{G}_{0}(\mathbf{q}) &= \tau + \tau_{d} + \mathrm{F}(\mathbf{q}, \boldsymbol{\dot{q}}, \boldsymbol{\ddot{q}}) \ (1.1) \\ \text{where F}(\mathbf{q}, \boldsymbol{\dot{q}}, \boldsymbol{\ddot{q}}) &= -\Delta \mathrm{M}(\mathbf{q}) - \Delta \mathrm{C}(\mathbf{q}, \boldsymbol{\dot{q}}) - \Delta \mathrm{G}(\mathbf{q}) \in \mathbb{R}^{n} \text{is the lumped system uncertainty which is} \end{aligned}$

bounded by the following function

 $\|F(\mathbf{q}, \dot{\mathbf{q}}, \ddot{\mathbf{q}})\| \le \rho_0 + \rho_1 \|\mathbf{q}\| + \rho_2 \|\dot{\mathbf{q}}\|^2 (1.2)$

where ρ_0 , ρ_1 and ρ_2 are positive constants.

Suppose the control objective is to make the robotic manipulator track a reference trajectory. Let q_d and q be the

www.ijser.in ISSN (Online): 2347-3878 Volume 2 Issue 3, March 2014

desired and actual position vectors. The tracking error and its derivatives are defined as

$$\mathbf{e} = \mathbf{q} - \mathbf{q}_{d}, \, \dot{\mathbf{e}} = \dot{\mathbf{q}} - \dot{\mathbf{q}}_{d} \text{ and } \, \ddot{\mathbf{e}} = \ddot{\mathbf{q}} - \ddot{\mathbf{q}}_{d} \text{ Using (1.1)},$$

$$\dot{\mathbf{e}} = M_{0}^{-1} (\mathbf{q}) [\mathbf{\tau} + \boldsymbol{\tau}_{d} + \mathbf{F}(\mathbf{q}, \, \dot{\mathbf{q}}, \, \ddot{\mathbf{q}}) - C_{0}(\mathbf{q}, \, \dot{\mathbf{q}}) \dot{\mathbf{q}} - G_{0}(\mathbf{q})] - \ddot{\mathbf{q}}_{d}$$

(1.3)

The time derivative of (1.3) yields $\frac{d}{dt}\ddot{e} = M_0^{-1}(q)[\dot{\tau} - \frac{d}{dt}(C_0(q, \dot{q})\dot{q} + G_0(q))] + M_0^{-1}(q)[\tau - C_0(q, \dot{q})\dot{q} - G_0(q)] - \frac{d}{dt}\ddot{q}_d + M_0^{-1}(q)\dot{\tau}_d + M_0^{-1}(q)\dot{F}(q, \dot{q}, \dot{q})$ $\ddot{q}) + M_0^{-1}(q)\tau_d + M_0^{-1}(q)F(q, \dot{q}, \ddot{q}) = M_0^{-1}(q)[\dot{\tau} - \frac{d}{dt}(C_0(q, \dot{q}) + G_0(q))] + M_0^{-1}(q)[\tau - C_0(q, \dot{q})\dot{q} - G_0(q)]\frac{d}{dt}\ddot{q}_d + F(q, \dot{q}, \ddot{q}) (1.4)$ where $\vec{F}(q, \dot{q}, \ddot{q}) = M_0^{-1}(q)\dot{\tau}_d + M_0^{-1}(q)\dot{F}(q, \dot{q}, \ddot{q}) + M_0^{-1}(q)\tau_d + M_0^{-1}(q)\dot{F}(q, \dot{q}, \ddot{q}) + M_0^{-1}(q)\tau_d + M_0^{-1}(q)F(q, \dot{q}, \ddot{q})$

such that, $\overline{F}(q, \dot{q}, \ddot{q}) \leq \overline{B_0} + \overline{B_1} ||q|| + \overline{B_2} ||\dot{q}||^2 (1.5)$

Here $\overline{B_0}$, $\overline{B_1}$ and $\overline{B_2}$ are positive constants.

Remark 5:5: The assumptions in the above inequalities are valid as the input disturbance $\tau_{\vec{a}}$ is assumed to be bounded, i.e. $\|\tau_{\vec{a}}\| < \chi$ where χ is a positive constant. Furthermore, the modeling

uncertainity F(q, \dot{q} , \ddot{q}) is also bounded by the assumption $\|F(q, \dot{q}, \ddot{q})\| \le \rho_0 + \rho_1 \|q\| + \rho_2 \|\ddot{q}\|^2$.

Let us consider the linear sliding surface as, s = $\dot{\boldsymbol{e}}$ + ce (1.6)

where $c = diag(c_1, ..., c_n)$ is a design matrix. The first and second derivative of (1.6) can be obtained as,

$$\dot{\mathbf{S}} = \ddot{\mathbf{e}} + c\dot{\mathbf{e}}$$
$$\ddot{\mathbf{S}} = \frac{d}{dt}\ddot{\mathbf{e}} + c\ddot{\mathbf{e}} = \frac{d}{dt}(\ddot{\mathbf{q}} - \ddot{\mathbf{q}}_{d}) + c\ddot{\mathbf{e}}$$

The nonsingular terminal sliding manifold (NTSM) for an n-link robotic manipulator is chosen as

$$\sigma = s + \beta s^{(\underline{p})} (1.7)$$

where Here $\beta = \text{diag}(\beta_1, \beta_2, ..., \beta_n)$ is a design matrix.

Taking the derivative of (1.7) yields

$$\dot{\boldsymbol{\sigma}} = \dot{\boldsymbol{s}} + \beta(\boldsymbol{p}/\boldsymbol{q})\boldsymbol{s}^{\left(\frac{p}{q}\right)-1}\boldsymbol{\ddot{s}}$$
$$= \beta(\boldsymbol{p}/\boldsymbol{q})\boldsymbol{s}^{\left(\frac{p}{q}\right)-1}(\boldsymbol{\ddot{s}} + (\boldsymbol{q}/\boldsymbol{p})\boldsymbol{\beta}^{-1}\boldsymbol{\dot{s}}^{2-\left(\frac{p}{q}\right)}) (1.8)$$

For an n-link robotic manipulator (1.0), if the NTSM manifold is chosen as (1.7), then the tracking error e will converge to zero if the time derivative of the control input is selected as, $\mathbf{\dot{\tau}} = \mathbf{\dot{u}}_0 + \mathbf{\dot{u}}_1 (1.9)$ 2.2 Adaptive Terminal Sliding Mode Controller

where,

$$\dot{u_0} = M_0(q) \frac{d}{dt} \ddot{q_d} + \frac{d}{dt} [$$

 $C_0(q, \dot{q}) \dot{q} + G_0(q)] -$
 $(\left(\frac{q}{p}\right) \beta^{-1} M_0 \dot{s}^{2-\left(\frac{p}{q}\right)}) - c M_0 \ddot{e} - M_0 M_0^{i-1} (\tau - C_0(q, \dot{q}) \dot{q} - G_0(q))$
(2.0)
 $\dot{u_1} = -K^+ M_0(q) \sigma - M_0(q) (\overline{B_0} + \overline{B_1} ||q|| + \overline{B_2} ||\dot{q}||^2) sign(\sigma)$ (2.1)
Here $K^+ = diag(K_1^+ \dots K_n^+)$ is a positive matrix.

Defining the adaptation error as $\overline{B_0}$ = $\overline{B_0} - \overline{B_0}$, $\overline{B_1} = \overline{B_1} - \overline{B_1}$ and $\overline{B_2} = \overline{B_2} - \overline{B_2}$, the parameters $\overline{B_0}$, $\overline{B_1}$, $\overline{B_2}$ are to be estimated by using the adaptation law.

$$\begin{split} \frac{\dot{F}_{q}}{B_{0}} &= \frac{1}{v_{0}} \left(\frac{p}{q}\right) \|\beta\| \left\| s^{\left(\frac{p}{q}\right)-1} \sigma \right\| (2.2) \\ \frac{\dot{F}_{1}}{B_{1}-v_{1}} \left(\frac{p}{q}\right) \|\beta\| \left\| s^{\left(\frac{p}{q}\right)-1} \sigma \right\| \|q\| (2.3) \\ \frac{\dot{F}_{2}}{B_{2}} &= \frac{1}{v_{2}} \left(\frac{p}{q}\right) \|\beta\| \left\| s^{\left(\frac{p}{q}\right)-1} \sigma \right\| \|\dot{q}\|^{2} (2.4) \end{split}$$

Where v_0, v_1, v_2 are the positive tuning parameters. The dead zone technique is used to modify the adaptive tuning law as

$$\begin{split} \frac{1}{B_0} &= \left\{ \frac{1}{v_0} \begin{pmatrix} p \\ q \end{pmatrix} \| \beta \| \left\| s^{\left(\frac{p}{q} \right) - 1} \sigma \right\|, \| \sigma \| \ge \varepsilon \\ 0, \| \sigma \| < \varepsilon \\ \frac{1}{B_1} &= \left\{ \frac{1}{v_1} \begin{pmatrix} p \\ q \end{pmatrix} \| \beta \| \left\| s^{\left(\frac{p}{q} \right) - 1} \sigma \right\| \| q \|, \| \sigma \| \ge \varepsilon \\ 0, \| \sigma \| < \varepsilon \end{split}$$

$$\frac{\dot{\overline{B}}_2}{\ddot{B}_2} = \left\{\frac{1}{v_2} \left(\frac{p}{q}\right) \|\beta\| \left\| s^{\left(\frac{p}{q}\right) - 1} \sigma \right\| \|\dot{q}\|^2, \|\sigma\| \ge \varepsilon$$

 $0, \|\sigma\| \leq \mathfrak{E}(2.5)$

where ε is a small positive constant.

Now, the adaptive terminal sliding mode control law for the robotic manipulator is obtained as,

$$\dot{u_1} = -K^+ M_0(q)\sigma - M_0(q) (\overline{B_0} + \overline{B_1} || q || + \overline{B_2} || \dot{q} ||^2) sign(\sigma) (2.6)$$

A Lyapunov function is defined as $V = \frac{1}{2}\sigma^2$ and using the control law it is easy to find that,

$$V = \sigma \bar{\sigma}$$

= $\sigma [c\nabla F - k_1 \sigma - k_2 sign(\sigma)]$
= $\sigma [Q - k_1 \sigma - k_2 sign(\sigma)]$
 $\leq Q ||\sigma|| - k_2 ||\sigma|| \leq -\eta ||\sigma||$

ISSN (Online): 2347-3878 Volume 2 Issue 3, March 2014

Clearly, the above equation implies that if, $\mathbf{k_1} \ge 0$ and $\mathbf{k_2} > \mathbf{Q}$, the control law forces the sliding manifold σ to zero in finite time.

Using Lyapunov stability criterion,

The NTSM manifold σ can be shown to possess finite time reachability to zero which ensures that the tracking error of the robotic manipulator $e = q - q_d$ converges to zero in finite time.

3. Simulation Results

The proposed chattering free adaptive terminal sliding mode (TSM) controller is applied for trajectory tracking of a two-link rigid robotic manipulator shown in Fig.5.4. For the above two-link manipulator, the dynamic equation (5.27) has the following parameters,

$$\begin{split} \mathbf{M}(\mathbf{q}) &= \\ \begin{bmatrix} (m_1 + m_2)l_1^2 + m_2l_2^2 + 2m_2l_1l_2\cos(q_2) + J & m_2l_2^2 + m_2l_1l_2\cos(q_2) \\ & m_2l_2^2 + m_2l_1\cos(q_2) & m_2l_2^2 + J_2 \end{bmatrix} \\ \mathbf{C}(\mathbf{q}, \dot{\mathbf{q}}) \, \dot{\mathbf{q}} &= \begin{bmatrix} -m_2l_1l_2\sin(q_2)\dot{q}_2^2 - 2m_2l_1l_2\sin(q_2)\dot{q}_1\ddot{q}_2 \\ & m_2l_1l_2\sin(q_2)\dot{q}_2^2 \end{bmatrix} \end{split}$$

$$G(q) = \begin{bmatrix} (m_1 + m_2)l_1g\cos(q_1) + m_2l_2g\cos(q_1 + q_2) \\ m_2l_2\cos(q_1 + q_2) \end{bmatrix}$$



Figure 1.1: Configuration of a two-link robotic manipulator

Here $q(t) = [q_1(t), q_2(t)]^T$ is the angular position vector where $q_1(t) \& q_2(t)$ are the angular positions of joints 1 & 2. M(q) is the inertia matrix, C(q) \dot{q} is the centripetal Coriolis matrix. G(q) is the gravity vector and $\tau = [\tau_1, \tau_2]^T$ is the applied torque. The two-link robotic manipulator has four inner states $x_1(t) = q_1(t)$, $x_2(t) = \dot{q}_1(t)$, $x_2(t) = \dot{q}_1(t)$, $x_1(t) = q_1(t)$, $x_2(t) = \dot{q}_2(t)$, $x_4(t) = \dot{q}_2(t)$, two output states $y_1(t) = q_1(t)$ and $y_2(t) = q_2(t)$ and two inputs $u_1(t) = \tau_1$ and $u_2(t) = \tau_2$. Friction terms are ignored. Table 1.0 lists the

physical parameters of the two-link robotic manipulator considered in the simulation study

Symbol	Definition	value
l_1	Length of the first link	1m
l_2	Length of the second link	0.85m
J_1	Moment of inertia of the D.C. motor 1	5kg - m
J_2	Moment of inertia of the D.C. motor 2	5kg - m
m_1	Mass of the link 1	0.5kg
m_2	Mass of link 2	1.5kg
\hat{m}_1	Nominal Mass of link 1	0.4kg
\hat{m}_2	Nominal Mass of link 2	1.2kg
g	Gravitational constant	$9.81m/s^2$

Table 1.0: Physical parameters of two-link robotic manipulator

The reference signals are $q_{d1} = 1.25 - (7/5)e^{-t} + (7/20)e^{-t}$ and $q_{d2} = 1.25 - e^{-t} - (1/4)e^{-4t}$. The inertial states are selected as $q_1(0) = 0, q_2(0) = 2.5, \dot{q}_1(0) = 0, \dot{q}_2(0) = 0$. The external disturbances considered are $\tau_{d1} = 2 \sin t + 0.5 \sin(200\pi t)$ and $\tau_{d2} = 2\cos 2t + 0.5\sin(200\pi t)$. The parameters of the controller selected proposed are as $p = 5, q = 3, \beta = diag(0.023, 0.023), c = diag(45, 45)$ and $K^{\dagger} = diag(60, 60)$

The simulations are carried out in MATLAB – Simulink platform by using ODE 4 solver with a fixed step size of 0.005sec.

The tracking response and control inputs obtained by using the NTSM controller.



Figure 1.2: Output tracking response of Joint 1 & Joint 2 with the controller

International Journal of Scientific Engineering and Research (IJSER)

www.ijser.in ISSN (Online): 2347-3878 Volume 2 Issue 3, March 2014



Figure 1.3: Control input of Joint 1 & Joint 2 with proposed controller

Simulation results obtained by applying the proposed adaptive TSM control laws (2.0) and (2.6) are shown in Fig. 1.4 - Fig. 1.7. It is observed from Fig. 1.4 that both the joints 1 and 2 track the reference trajectory faithfully. The control inputs applied to both the joints show no chattering as is evident in Fig. 1.5. The convergence plots of the estimated parameters $\hat{B}_0, \hat{B}_1, \hat{B}_2$ are shown in Fig. 1.6. The sliding surfaces and the sliding manifolds are plotted in Fig. 1.7 which confirms that these converge to zero quickly.



Figure 1.4: Output tracking response of Joint 1 & Joint 2 with the controller



Figure 1.5: Control input of Joint 1 & Joint 2 with proposed controller



Figure 1.6: Estimated parameters \vec{B}_0 , $\vec{B}_1 \& \vec{B}_2$ using the proposed adaptive tuning method

International Journal of Scientific Engineering and Research (IJSER)

www.ijser.in ISSN (Online): 2347-3878 Volume 2 Issue 3, March 2014



Figure 1.7: Sliding surfaces and sliding manifolds using the proposed controller

The output and input performances of the proposed adaptive TSM controller as well as the controllers designed by Feng et al. for the two-link robotic manipulator are tabulated in Table 1.2. It is noted that the proposed adaptive TSM controller offers comparable tracking performance by applying a smoother control input having minimal total variation as compared to the controllers designed by Feng et al. Moreover, the overall control energy spent in the case of the proposed adaptive TSM controller is not more than those in the other methods.

Table 1.1: Comparison of controller performanc
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Controller Performance							
Types Of Control	IAE	Total Variation	2-norm of input				
Fana at al	Joint 1	14.8 5	205.01	72.22			
reng et al.	Joint 2	7.22	127.92	207.79			
Proposed adaptive	Joint 1	7.01	114.29	114.61			
TSM controller	Joint 2	4.05	74.02	140.03			

4. Conclusion

An adaptive terminal sliding mode (TSM) controller is proposed where the nonsingular terminal sliding manifold guarantees fast and finite time convergence. The proposed adaptive TSM controller is successfully applied for stabilization. Trajectory tracking of a two-link robotic manipulator which is a nonlinear system with mismatched uncertainty is considered which demonstrates the efficiency of the proposed control strategy. Simulations performed on a twolink robotic manipulator demonstrate the effectiveness of the proposed controller.

5. Future Scope

Discrete Sliding Mode Controllers will be easier to implement as compared to microcontrollers and digital signal processors (DSPs) which can also be used to control a huge number of continuous systems. The proposed design method may be extended by using intelligent controllers based on Neural Networks and Fuzzy Logic to incorporate flexibility and intelligence.

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